

Simple argument from foreknowledge—I can't but eat lobster tonight!

Let $p =$ I will eat lobster tonight. Suppose someone, x , knows that p

- F1. x knows that p
 F2. If x knows that p , x can't be wrong
F3. If it were possible that not- p , x could be wrong
 F4. It isn't possible that not- p

Solution: distinguish between: F2'. $K_x p \rightarrow \Box p$ and: F2''. $\Box(K_x p \rightarrow p)$

Argument from God's necessary omniscience

- G1. p
G2. God is necessarily omniscient
 G3. God necessarily knows that p G1, G2 \times modus ponens
G4. Necessarily if God knows that p , then p Factivity of knowledge
 G5. Necessarily p G3, G4 by modal logic

Solution: distinguish between: G2'. $\forall p(p \rightarrow \Box K_{God} p)$ and: G2'' $\Box \forall p(p \rightarrow K_{God} p)$

The Master Argument of Diodorus Cronus

- D1. Whenever anything has been the case, it cannot but have been the case
 D2. Whatever is entailed by anything possible is itself possible
 D3. When anything is the case, it has never been the case that it will not be the case
D4. When anything neither is nor will be the case, it has been the case that it won't be the case
 D5. If something neither is nor will be the case, it is impossible that it should be the case

- D1. $Pp \rightarrow \neg \Diamond \neg Pp$
 D2. $(\Diamond p \wedge \Box(p \rightarrow q)) \rightarrow \Diamond q$
 D3. $p \rightarrow \neg P \neg Fp$
D4. $(\neg p \wedge \neg Fp) \rightarrow P \neg Fp$
 D5. $(\neg p \wedge \neg Fp) \rightarrow \neg \Diamond p$

To deduce D5 from D1-4 , suppose	1	$\neg p \wedge \neg Fp$
$\neg p \wedge \neg Fp + D4 \times$ modus ponens \Rightarrow	2	$P \rightarrow Fp$
Substitute $\neg Fp$ for p in D1 \Rightarrow	3	$P \rightarrow Fp \rightarrow \neg \Diamond \neg P \rightarrow Fp$
2 + 3 \times modus ponens \Rightarrow	4	$\neg \Diamond \neg P \rightarrow Fp$
For reductio, assume	5	$\Diamond p$
5 + D3 \times D2 \Rightarrow	6	$\Diamond \neg P \rightarrow Fp$
4 + 6 \times reductio \Rightarrow	7	$\neg \Diamond p$
1-7 \times conditional proof \Rightarrow	D5	$(\neg p \wedge \neg Fp) \rightarrow \neg \Diamond p$

Rejecting D4 Indeterminism & 3-valued logic

	q				q				$\neg p$	
	$p \wedge q$	t	n	f	$p \rightarrow q$	t	n	f	t	f
	t	t	n	f	t	t	n	f	t	f
p	n	n	n	f	p	n	t	n	n	n
	f	f	f	f	f	t	t	t	f	t

The structure of time

Assuming discreteness of time, we can argue:

suppose	1	$\neg P \rightarrow Fp$	at t	
suppose	2	$\neg Fp$	at $t - 1$	
then	3	$P \rightarrow Fp$	at t	
so	4	$\neg \neg Fp$	at $t - 1$	1,3 \times reductio
so	5	Fp	at $t - 1$	4 \times DNE
so either	6	p at t or p at $t+n$ for some $n \geq 1$		5
either way	7	$p \vee Fp$	at t	
so	8	$\neg(\neg p \wedge \neg Fp)$	at t	7 \times de Morgan law
hence	9	$\neg P \rightarrow Fp \rightarrow \neg(\neg p \wedge \neg Fp)$		1-8 \times conditional proof
hence	10	$\neg p \wedge \neg Fp \rightarrow P \rightarrow Fp$		9 \times contraposition

But without assuming discreteness, the argument breaks down at 6. We must replace 2 by

2' $\neg Fp$ at $t - j$ for $j > 0$

which gives 6' p at t' for $t' > t - j$ instead of 6

We must then consider two alternatives: $t' < t$ or $t' \geq t$

—we can prove $p \vee Fp$ at t from $t' \geq t$, but *not* from $t' < t$